## Séminaire de Probabilités et Statistiques

Mardi 26 Septembre à 14h00

Laboratoire Dieudonné Salle de Conférences

## Mario Maurelli

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Regularization by noise for scalar conservation laws

We say that a regularization by noise phenomenon occurs for a possibly ill-posed differential equation if this equation becomes well-posed (in a pathwise sense) under addition of noise. Most of the results in this direction are limited to SDEs and associated linear SPDEs.

In this talk, we show a regularization by noise result for a nonlinear SPDE, namely a stochastic scalar conservation law on  $\mathbb{R}^d$  with a space-irregular flux :

$$\partial_t v + b \cdot \nabla[v^2] + \nabla v \circ \dot{W} = 0,$$

where b = b(x) is a given deterministic, possibly irregular vector field, W is a *d*-dimensional Brownian motion ( $\circ$  denotes Stratonovich integration) and  $v = v(t, x, \omega)$  is the scalar solution. More precisely we prove that, under suitable Sobolev assumptions on b and integrability assumptions on its divergence, the equation admits a unique entropy solution. The result is false without noise.

The proof of uniqueness is based on a careful combination of arguments used in the linear case : first we show the renormalization property for the kinetic formulation of the equation, then we use second order PDE estimates and a duality argument to conclude.

If time permits, we will discuss also some open questions.

(Joint work with Benjamin Gess)